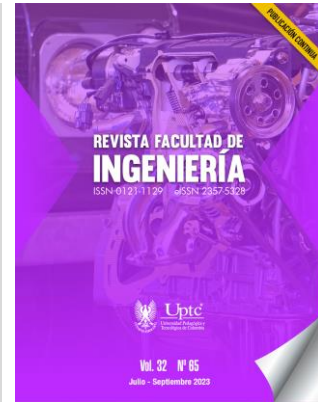


Revista Facultad de Ingeniería

Journal Homepage: <https://revistas.uptc.edu.co/index.php/ingenieria>



2D Gradient Algorithms for Noise Reduction in Radiological Images

Jhonatan Collazos-Ramirez¹

Pablo-Emilio Jojoa²

Juan-Pablo Hoyos-Sanchez³

Received: July 03, 2023

Accepted: August 31, 2023

Published: September 04, 2023

Citation: J. Collazos-Ramírez, P.-E. Jojoa, J.-P. Hoyos-Sánchez, "2D Gradient Algorithms for Noise Reduction in Radiological Images," *Revista Facultad de Ingeniería*, vol. 32, no. 65, e16178, 2023. <https://doi.org/10.19053/01211129.v32.n65.2023.16178>

Abstract

In areas such as biomedical image processing, the techniques or methods used to recover the content in noise-contaminated signals are essential. One of them has been adaptive filtering, which, by adjusting to the desired signal through real-time updating of the coefficients, allows improvement and deconvolution in the recovery of degraded or contaminated images, attracting the attention of researchers in inverse problems. In this paper, the 2D-AR γ gradient algorithm is used in noise

¹ MSc. Universidad del Cauca (Popayán-Cauca, Colombia). jcollazos@unicauca.edu.co. ORCID: [0000-0003-3822-7895](https://orcid.org/0000-0003-3822-7895)

² Ph. D. Universidad del Cauca (Popayán-Cauca, Colombia). pjojoa@unicauca.edu.co. ORCID: [0000-0002-8461-4063](https://orcid.org/0000-0002-8461-4063)

³ Ph. D. Universidad Nacional de Colombia (La Paz-Cesar, Colombia). jhoyoss@unal.edu.co. ORCID: [0000-0002-1844-9127](https://orcid.org/0000-0002-1844-9127)



reduction in dental radiological images, for which simulations are performed to obtain the best configuration of the hyperparameters, and a statistical analysis of the values obtained is performed. Based on the simulation results and the established metrics, it is demonstrated that the algorithm achieves a slightly higher noise reduction than the other 2D gradient algorithms (LMS and NLMS).

Keywords: 2D adaptive filter; adaptive two-dimensional filter; gradient algorithm; noise cancellation; radiological images; signal processing.

Algoritmo de gradiente 2D para la reducción del ruido en imágenes radiológicas

Resumen

En áreas como el procesamiento de imágenes biomédicas las técnicas o métodos para recuperar el contenido en señales que están contaminadas con ruido son indispensables. Una de ellas ha sido el filtrado adaptativo que, al ajustarse a la señal deseada a través de la actualización en tiempo real de los coeficientes permite el mejoramiento y la deconvolución en la recuperación de imágenes degradadas o contaminadas, logrando atraer la atención de investigadores en problemas inversos. En este artículo el algoritmo del gradiente 2D-AR γ es utilizado en la reducción de ruido en imágenes radiológicas dentales, para lo cual se realizan simulaciones para obtener la mejor configuración de los hiperparámetros y se realiza un análisis estadístico de los valores obtenidos. Con base en los resultados de la simulación y las métricas establecidas, se demuestra que el algoritmo logra una reducción del ruido estadísticamente superior que los otros algoritmos del gradiente 2D (LMS y NLMS).

Palabras clave: 2D filtro adaptativo; algoritmo gradiente; cancelación de ruido; filtro bidimensional adaptativo; imágenes radiológicas; procesamiento de señales.

Algoritmo de gradiente 2D para redução de ruído em imagens radiológicas

Resumo

Em áreas como processamento de imagens biomédicas, técnicas ou métodos para recuperar o conteúdo de sinais contaminados com ruído são essenciais. Uma delas

tem sido a filtragem adaptativa que, ao se ajustar ao sinal desejado através da atualização em tempo real dos coeficientes, permite melhoria e desconvolução na recuperação de imagens degradadas ou contaminadas, atraindo a atenção de pesquisadores em dificuldades. Neste artigo é utilizado o algoritmo de gradiente 2D-AR γ para redução de ruído em imagens radiológicas dentárias, para o qual são realizadas simulações para obter a melhor configuração dos hiperparâmetros e é realizada uma análise estatística dos valores obtidos. Com base nos resultados da simulação e nas métricas estabelecidas, mostra-se que o algoritmo atinge uma redução de ruído estatisticamente superior aos outros algoritmos de gradiente 2D (LMS e NLMS).

Palavras-chave: 2D filtro adaptativo; algoritmo de gradiente; cancelamento de ruído; filtro bidimensional adaptativo; imagens radiológicas; processamento de sinais.

I. INTRODUCTION

X-ray images play a fundamental role in image processing, particularly in the field of medicine. These images are vital, as they are used as a primary clinical tool for disease interpretation and accurate pathological decision-making. In recent years, there have been significant advances in the technologies employed in clinical settings, enabling the acquisition of X-ray images with millimeter-scale resolution and providing a detailed view of internal anatomical structures. Thanks to this improvement in image quality, it is possible to perform an exhaustive analysis of these images and, consequently, develop image-guided therapies based on computer-assisted diagnosis. This combination of cutting-edge technology and computational analysis has opened new possibilities in medicine, allowing for a more precise interpretation of X-ray images and facilitating the planning of more effective and personalized treatments for each patient [1, 11, 12].

Since its discovery by Röntgen, X-rays have been the subject of extensive research in various fields. One of the earliest applications of X-rays was in the medical field to gather information from inside the body without dissection. Over the years, significant advancements have been made in medical imaging, leading to the development of various systems capable of capturing moving images, mainly focused on the cardiovascular system and 3D imaging by computed tomography [2,13].

The interaction of X-rays with the human body to obtain the desired image is summarized in Figure 1. In this process, an X-ray beam is generated, which passes through the object in question, in our case, the human body, and is partially absorbed by internal structures in a phenomenon known as attenuation. On the opposite side of the body, a detector absorbs the attenuated X-rays and generates an image showing a shadow representation of the bones and soft tissues (Figure 1 (a)). However, due to the random impact of attenuated X-ray photons on the receiver plate during a given time interval, an uneven distribution of photons on the surface of the receiver occurs (Figure 1 (b)). This phenomenon results in irregular artifacts in the image that produce noise [3,14]. It is important to consider these factors to understand the limitations and challenges associated with X-ray image acquisition

so that processing methods and noise reduction techniques can be improved to obtain clearer and more accurate images.

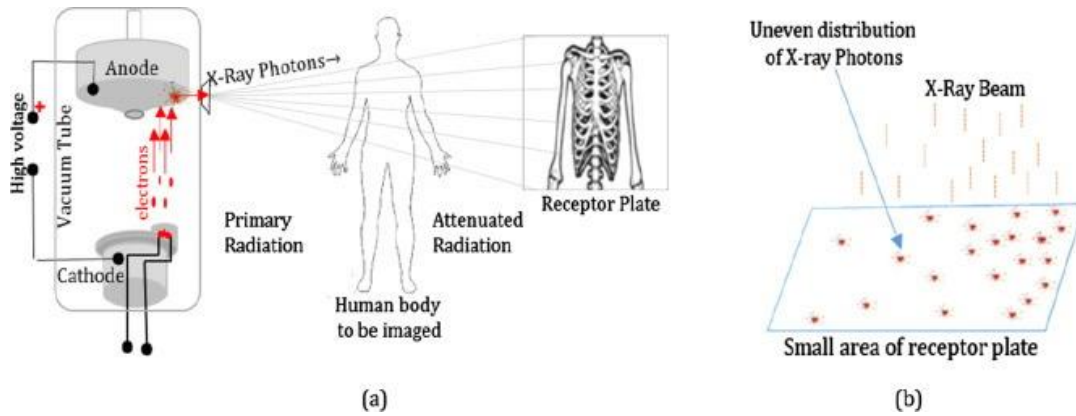


Fig. 1. (a) X-ray imaging modality. (b) Uneven distribution of X-ray photons in a small area of the receptor plate [3].

X-rays, due to their high energy, can negatively affect the human body because it is continuously concentrated, which is particularly harmful in pediatric radiology [2]. In order to reduce the risk of exposure, methods have been developed to use low doses of X-rays, which involves reduced photon information reaching the detector, consequently degrading image quality. In other words, there is a trade-off between noise reduction and information loss. Therefore, selecting an efficient filtering algorithm [3] is required to improve image quality rather than increasing the radiation dose. Denoising algorithms [4,14,15] offer a promising solution in this context. Considering the properties of gradient-based algorithms [5], such as 2D-LMS and 2D-NLMS, in this paper, noise reduction in dental radiological images is investigated using the 2D-AR γ algorithm [6].

II. METHODOLOGY

According to [6], the 2D-AR γ algorithm is governed by the following matrix equations:

$$e_n = \mathbf{X}_n^T \mathbf{W}_n - d_n \quad (1)$$

$$g_n = \frac{e_j + \gamma \mathbf{X}_n^T \mathbf{W}_n}{1 + \alpha \gamma m_1 \mathbf{X}_n^T \mathbf{X}_n} - d_n \quad (2)$$

$$\mathbf{Q}_{n+1} = \frac{\gamma}{\alpha + \gamma} [\mathbf{Q}_n - \alpha m_1 g_n \mathbf{X}_n] \quad (3)$$

$$\mathbf{W}_{n+1} = \mathbf{W}_n + \alpha \mathbf{Q}_n \quad (4)$$

where for the time instant $[n]$:

\mathbf{X}_n : Matrix of the input signal

\mathbf{W}_n : Matrix of adaptive filter coefficients

d_n : Scalar corresponding to the desired signal

e_n : Scalar corresponding to the measurement error

g_n : Auxiliary scalar

\mathbf{Q}_n : Auxiliary Matrix

α, γ, m_1 : Adjustment parameters

For the noise cancellation configuration of the 2D-AR γ filter, the block diagram scheme shown in Figure 2 was used.

The main signal $\mathbf{d}(\mathbf{n}_1, \mathbf{n}_2)$ is a combination of the desired signal $\mathbf{s}(\mathbf{n}_1, \mathbf{n}_2)$ and noise $\mathbf{x}(\mathbf{n}_1, \mathbf{n}_2)$. The reference signal $x_1(\mathbf{n}_1, \mathbf{n}_2)$ is the noise correlated with the noise in the main signal. The 2D adaptive filter aims to reduce the noisy signal using the equation:

$$e(\mathbf{n}_1, \mathbf{n}_2) = d(\mathbf{n}_1, \mathbf{n}_2) - y(\mathbf{n}_1, \mathbf{n}_2) \approx s(\mathbf{n}_1, \mathbf{n}_2) \quad (5)$$

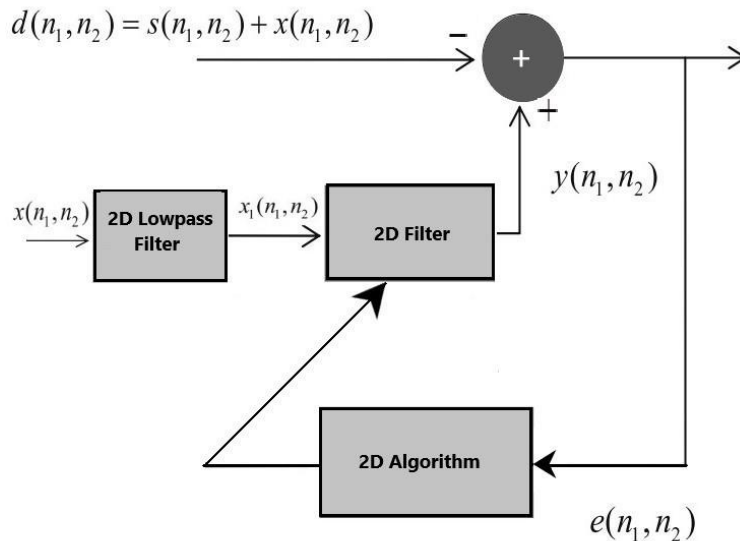


Fig. 2. Configuration of 2D adaptive noise reduction.

After the convergence of the filter coefficients, $e(\mathbf{n}_1, \mathbf{n}_2)$ will be the estimation of the desired signal. In this simulation, white Gaussian noise with zero mean and unit

variance $x(\mathbf{n}_1, \mathbf{n}_2)$ is added to the image to create a noisy image, where the Peak Signal-to-Noise Ratio (PSNR) is set to 0 dB.

Taking the works [7], [8] as a reference in the configuration of the 2D low-pass filter in Figure 2, the reference signal $x_1(\mathbf{n}_1, \mathbf{n}_2)$ is generated by passing white Gaussian noise with zero mean and unit variance through a 2D low-pass filter.

To determine the best parameters for the 2D-AR γ algorithm, the following phases were carried out:

1. Variation of α and γ with m_1 fixed.
2. Variation of α and m_1 with γ fixed.
3. Variation of m_1 and γ with α fixed.

The variation of the parameters was performed between 0 and 1000 for each image. Once the values where the PSNR is higher were identified, we proceeded to search near those same parameters for new values that allowed us to obtain an even higher PSNR. The order of the 2D adaptive filter was set to $N_1 = N_2 = 6$. The algorithm was run once. Table 1 shows the optimal values found in the three phases of the procedure.

Table 1. Parameters comparison.

Phase	Image	Optimal Parameters			PSNR(OUT)
		γ	α	m_1	
1	1	0.001	0.81	0.001	2.4089
	29	0.11	0.11	0,01	2.4136
	58	0.11	0.11	0.01	2.4084
	116	0.31	0.11	0.011	2.3649
2	1	0.01	0.81	0.001	2.3649
	29	0.01	0.3	0.3	2.4142
	58	1	0.01	0.01	2.3738
	116	0.1	0.01	0.41	2.1954
3	1	0.9	1	10^{-4}	2.4136
	29	0.8	10^{-3}	10^{-4}	2.3807
	58	0.3	0.01	0.02	2.3787
	116	0.4	0.01	10^{-4}	2.3796

III. RESULTS

The functionality of the 2D adaptive algorithms is validated using real dental radiological images contaminated with Gaussian noise. The order of the 2D adaptive

filter is set to $N_1 = N_2 = 6$. The algorithm was run 20 times with different random seeds.

Figure 3 shows the radiological images used for the simulation. These images are available in an open-source database [9]. The access path to the images is as follows: DentalPanoramicXrays.zip → Images → 1.png, 29.png, 58.png, 116.png.

Table 2 presents some metrics used to compare the performance of the 2D adaptive filters in terms of image quality [3].

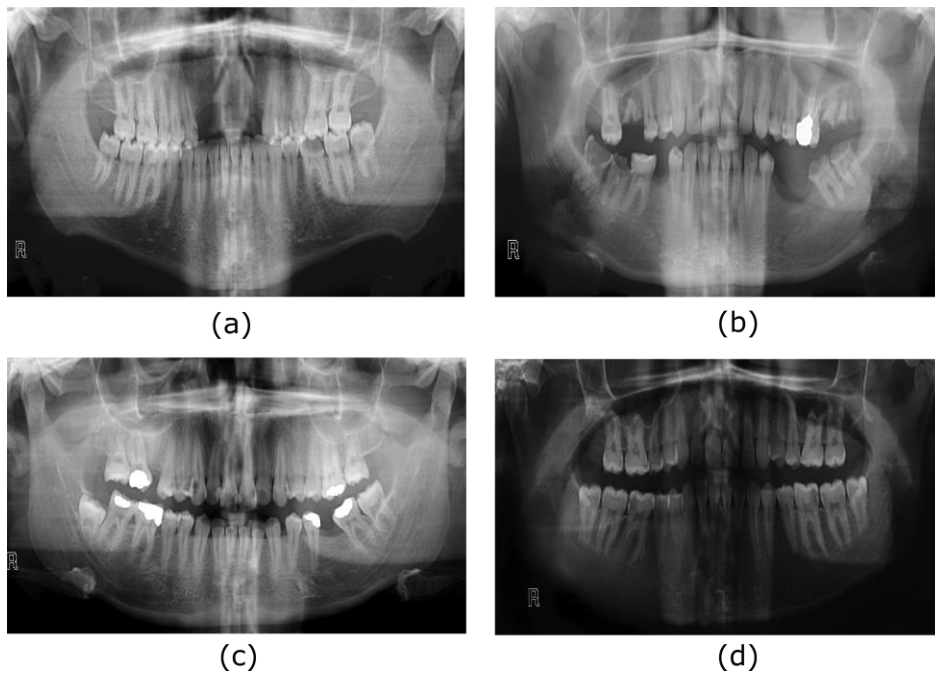


Fig. 3. Dental radiological images: (a) 1.png, (b) 29.png, (c) 58.png, (d) 116.png.

Where I is the original image and J is the filtered image, M_1 and M_2 are the dimensions of the image.

Table 2. Image quality measures [10].

Image quality metric	Formula
MSE	$\frac{1}{M_1 M_2} \sum_{i=1}^{M_1} \sum_{j=1}^{M_2} [I(i, j) - J(i, j)]^2$
RMSE	$\sqrt{\frac{1}{M_1 M_2} \sum_{i=1}^{M_1} \sum_{j=1}^{M_2} [I(i, j) - J(i, j)]^2}$

Image quality metric	Formula
SNR	$10 \log_{10} \frac{\sum_{i=1}^{M_1} \sum_{j=1}^{M_2} I^2(i, j)}{\sum_{i=1}^{M_1} \sum_{j=1}^{M_2} [I(i, j) - J(i, j)]^2}$
PSNR	$-10 \log_{10} \frac{\sum_{i=1}^{M_1} \sum_{j=1}^{M_2} [I(i, j) - J(i, j)]^2}{M_1 M_2}$

The Mean Square Error (MSE) is the average of differences between the filtered and the reference images. A high MSE value indicates a degraded image, while zero MSE represents a perfect image. On the other hand, the Root Mean Square Error (RMSE) quantifies the standard deviation of the points concerning the fitted regression line. It is the square root of the mean square error and provides information about the accuracy of the fit. The Signal-to-Noise Ratio (SNR) is defined as the ratio of the signal power to noise power. This measure reflects how noise affects the visual quality of an image. Finally, the Peak Signal-to-Noise Ratio (PSNR) is a widely used metric to evaluate the quality of a restored image when it has been affected by noise and blur. It is calculated as the ratio between the maximum possible signal and the mean square error of the restored image.

A high SNR value indicates a low level of noise. On the other hand, a low RMSE value represents better image quality since it reflects a smaller difference between the filtered and the reference images. Finally, a higher PSNR value corresponds to higher image quality, indicating less distortion than the original image. [3]. Table 3 shows that the 2D-AR γ algorithm consistently produces slightly better results across all metrics compared to the 2D-LMS and 2D-NLMS algorithms.

Table 3. Comparative quality measurement values.

Metric	Image	Algorithm		
		2D-LMS	2D-NLMS	2D- AR γ
MSE	1	0.0335	0.0313	0.0286
	29	0.0334	0.0313	0.0286
	58	0.0335	0.0313	0.0286
	116	0.0324	0.0307	0.0285
RMSE	1	0.1830	0.1769	0.1691
	29	0.1827	0.1768	0.1690
	58	0.1830	0.1769	0.1691

Metric	Image	Algorithm		
		2D-LMS	2D-NLMS	2D-AR γ
SNR	116	0.1801	0.1751	0.1688
	1	8.3327	8.6251	9.0187
	29	7.9170	8.2017	8.5942
	58	8.1910	8.4836	8.8780
	116	8.3139	7.9888	8.8332
PSNR	1	14.7527	15.0451	15.4387
	29	14.7647	15.0494	15.4420
	58	14.7509	15.0435	15.4379
	116	14.8919	15.1340	15.4502

ANOVA (Analysis of Variance) tests were conducted along with the Turkey HSD (Honest Significant Difference) test to achieve statistical validity. The results are presented in Table 4. Three comparison groups were formed: LMS vs. AR γ , NLMS vs. AR γ , and LMS vs. NLMS. For each comparison, the 95% confidence interval and the corresponding p-value are provided. A significant difference is observed when the p-value is less than 0.01, leading to the rejection of the null hypothesis. There is no difference between the values obtained by AR γ and the LMS and NLMS filters. From the table, we can identify significant differences for all metrics ($p \leq 0.001$), indicating the statistical validity of the algorithm's performance. Therefore, we can assert that the AR γ algorithm presents a better performance compared to the LMS and NLMS filters.

Table 4. Results of the ANOVA + Turkey HSD test.

Metric	Group	Confidence Interval (95%)	p-value
MSE	LMS vs. AR γ	(0.003923, 0.005326)	≤ 0.001
	NLMS vs. AR γ	(0.001873, 0.00327)	≤ 0.001
	LMS vs. NLMS	(-0.002751, -0.001348)	≤ 0.001
RMSE	LMS vs. AR γ	(0.01129, 0.01510)	≤ 0.001
	NLMS vs. AR γ	(0.005523, 0.009326)	≤ 0.001
	LMS vs. NLMS	(-0.007676, -0.003873)	≤ 0.001
SNR	LMS vs. AR γ	(-1.4593 y 0.24516)	≤ 0.001
	NLMS vs. AR γ	(-1.1508, 0.38207)	≤ 0.001
	LMS vs. NLMS	(-0.6897 y 1.6287)	≤ 0.001
PSNR	LMS vs. AR γ	(-0.7449, -0.5593)	≤ 0.001
	NLMS vs. AR γ	(-0.4669, -0.2814)	≤ 0.001
	LMS vs. NLMS	(0.1851, 0.3707)	≤ 0.001

Figure 4 depicts the fast convergence of the 2D adaptive filter algorithms, and the MSE values approach zero at the iteration near 200. This indicates a significant computational efficiency of the 2D adaptive filter algorithms.

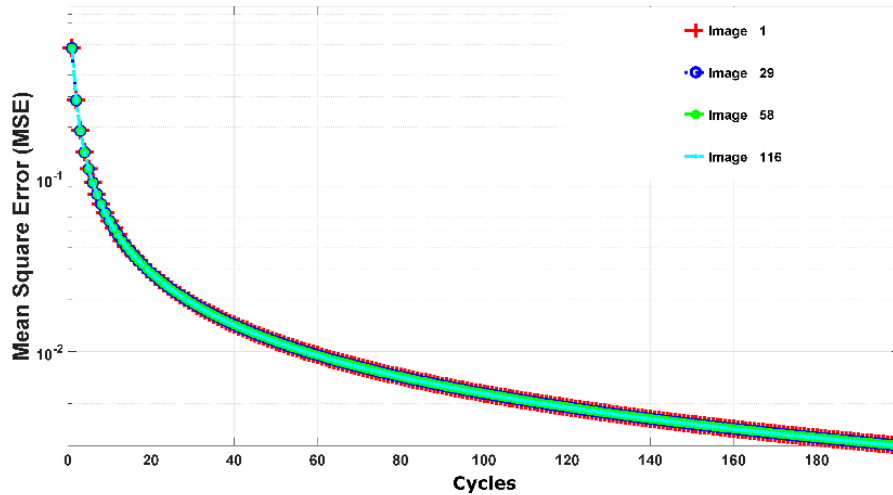


Fig. 4. Convergence characteristics of the 2D adaptive filter algorithm for all test images.

In the analysis of the output peak power performance of the 2D adaptive filter algorithms, different input PSNR values were used. Figure 5 shows the input and output PSNR values using the 2D-LMS, 2D-NLMS, and 2D-AR γ adaptive filter algorithms for various test images or changing noise conditions. It was observed that the performance of the 2D-AR γ adaptive filter algorithm was significantly more efficient in noise reduction compared to the other two algorithms. This was reflected in the output PSNR values, which indicated higher quality and lower distortion in the filtered images using the 2D-AR γ adaptive filter algorithm. Thus, the proposed algorithm demonstrates robustness against various noise conditions in the images, translating to the ability to handle different PSNR values in the input image.

2D Gradient Algorithms for Noise Reduction in Radiological Images

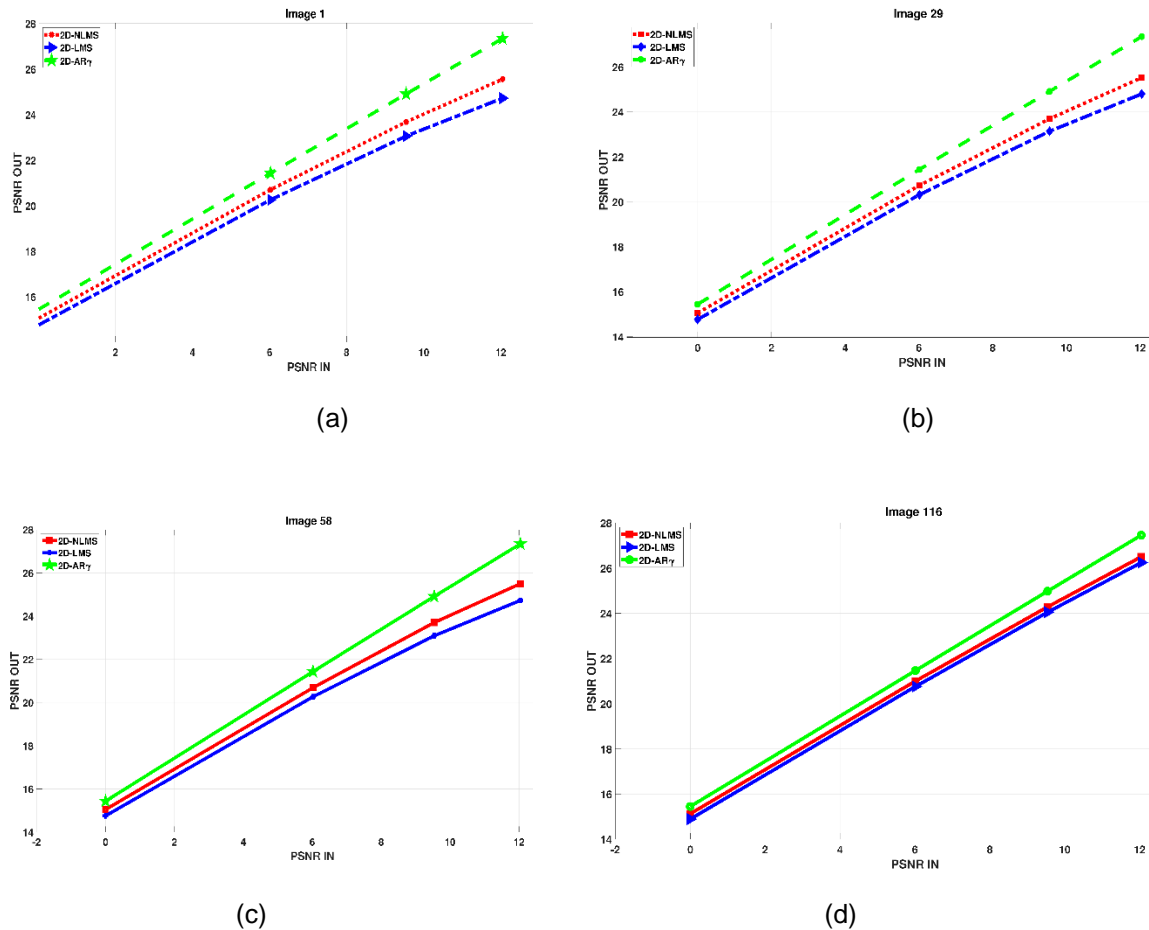


Fig. 5. Output PSNR versus input PSNR for 2D-LMS, 2D-NLMS, and 2D- AR γ . (a) image 1.png (b) image 29.png (c) image 58.png (d) image 116.png.

Finally, the radiological images restored using different adaptive filters are presented. Figures 6, 7, 8, and 9 show the noisy and restored images using different 2D adaptive filtering algorithms, respectively. From visual observation, it can be seen that the proposed filter produces a smoother version of the image and, thus, a slightly higher noise reduction compared to the LMS and 2D-NLMS algorithms. Furthermore, the proposed filter improves the visualization of the elements present in the image by more accurately highlighting transitions or edges. This enhancement means that details and structures of interest in the image become more discernible and can be appreciated with greater clarity.

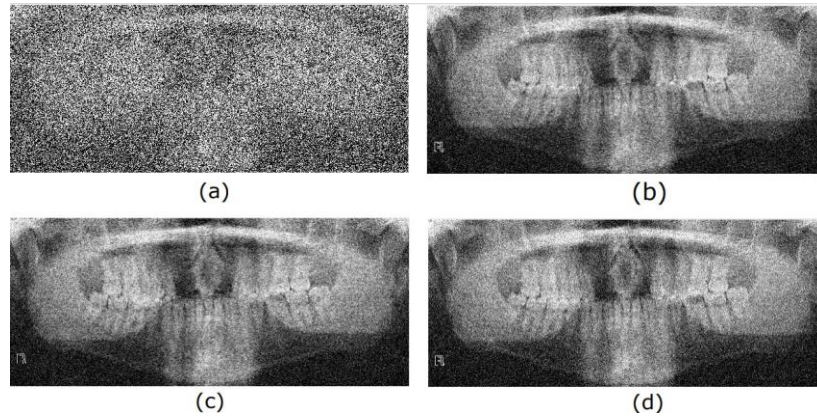


Fig. 6. Noise Reduction in Image 1.png (a) Noisy Image (b) 2D-LMS (c), 2D-NLMS, (d) 2D- AR γ .

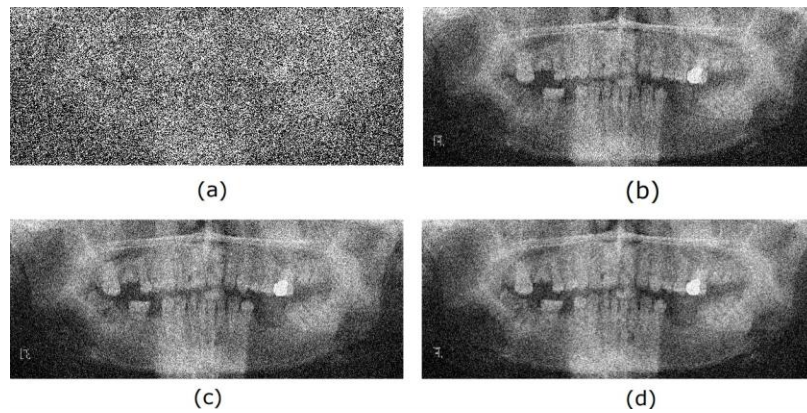


Fig. 7. Noise Reduction in Image 29.png (a) Noisy Image (b) 2D-LMS (c), 2D-NLMS, (d) 2D- AR γ .

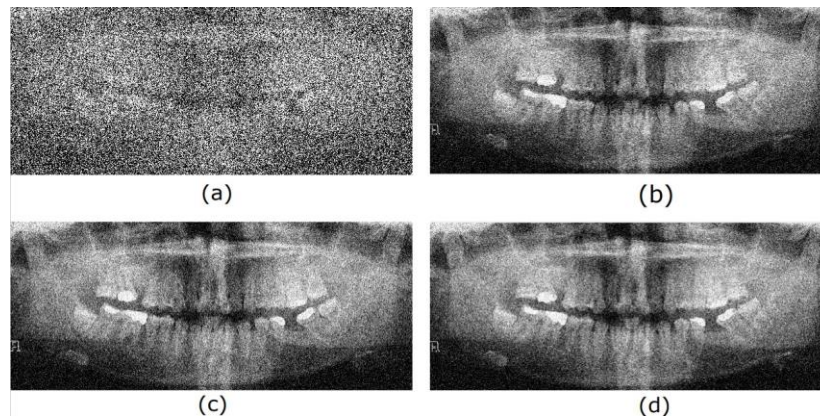


Fig. 8. Noise Reduction in Image 58.png (a) Noisy Image (b) 2D-LMS (c), 2D-NLMS, (d) 2D- AR γ .

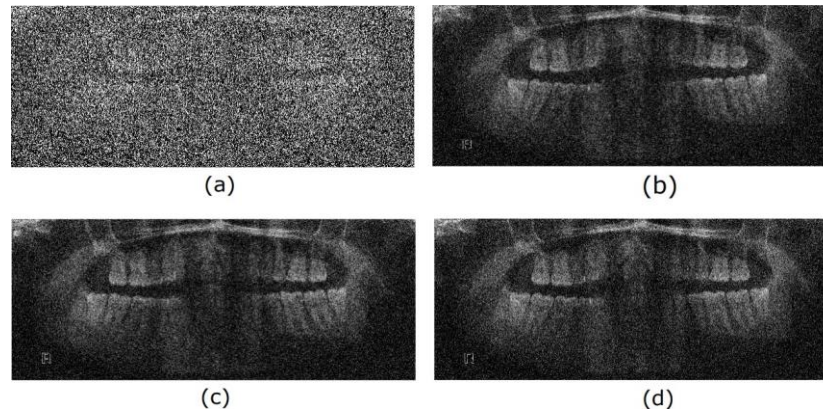


Fig. 9. Noise Reduction in Image 116.png (a) Noisy Image (b) 2D-LMS (c), 2D-NLMS, (d) 2D- $AR\gamma$.

IV. CONCLUSIONS

In this paper, for the first time, the use of the 2D- $AR\gamma$ algorithm in noise reduction in dental radiological images is proposed. Three calibration phases were conducted for algorithm development. The performance of the 2D- $AR\gamma$ adaptive filter algorithm was compared with that of other classical algorithms. To ensure a fair comparison, all conditions were determined according to recommendations from the literature. ANOVA and Turkey HSD analyses were performed on the obtained metric results, demonstrating statistically superior outcomes. In comparison with the LMS and 2D-NLMS algorithms, the proposed filter provides a favorable combination of noise reduction and enhanced visibility of elements in radiological images. These results support the efficacy and superior performance of the proposed adaptive filter in the context of radiological image restoration.

The application of this adaptive filter has the potential to contribute to higher quality and more accurate radiological images in dental diagnosis, which can have a positive impact on clinical practice and improve patient care.

AUTHORS' CONTRIBUTION

Jhonatan Collazos-Ramirez: Research, data analysis, implementation, writing—original draft.

Pablo-Emilio Jojoa: Research, supervision, methodology, writing—review and editing.

Juan-Pablo Hoyos-Sanchez: Research, supervision, methodology, writing—review and editing.

REFERENCES

- [1] F. Schopper, J. Ninkovic, R. Richter, G. Schaller, T. Selle, J. Treis, "High resolution X-ray imaging with pnCCDs," *Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment.*, vol. 912, pp. 11–15, 2018. <https://doi.org/10.1016/j.bspc.2022.104031>
- [2] S. Lee, M. S. Lee, M. G. Kang, "Poisson--Gaussian noise analysis and estimation for low-dose X-ray images in the NSCT domain," *Sensors*, vol. 18, no. 4, e1019, 2018. <https://doi.org/10.3390/s18041019>
- [3] T. B. Chandra, K. Verma, "Analysis of quantum noise-reducing filters on chest X-ray images: A review," *Measurement*, vol. 153, e107426, 2020. <https://doi.org/10.1016/j.measurement.2019.107426>
- [4] T. Kirti, K. Jitendra, S. Ashok, "Poisson noise reduction from X-ray images by region classification and response median filtering," *Sādhanā*, vol. 42, no. 6, pp. 855–863, 2017. <https://doi.org/10.1007/s12046-017-0654-4>
- [5] S. Kockanat, N. Karaboga, "A novel 2D-ABC adaptive filter algorithm: a comparative study," *Digital Signal Processing*, vol. 40, pp. 140–153, 2015. <https://doi.org/10.1016/j.dsp.2015.02.010>
- [6] J. Collazos Ramirez, P. E. Jojoa Gomez, J. P. Hoyos Sanchez, "Extension and Analysis of the ARG algorithm to 2D," *IEEE Latin America Transactions*, vol. 20, no. 12, pp. 2448-2454, 2022. <https://doi.org/10.1109/TLA.2022.9905613>
- [7] A. M. S. Esfand, S. Nikbakht, "Image denoising with two-dimensional adaptive filter algorithms", *Iranian Journal of Electrical and Electronic Engineering*, vol. 7, pp. 84-105, 2011.
- [8] M. S. E. Abadi, S. N. Aali, "The novel two-dimensional adaptive filter algorithms with the performance analysis," *Signal Processing*, vol. 103, pp. 348–366, 2014. <https://doi.org/10.1016/j.sigpro.2013.12.016>
- [9] A. Abdi, S. Kasaei, "Panoramic dental X-rays with segmented mandibles," *Mendeley Data*, v2, 2020. <https://doi:10.17632/hxt48yk462.2>
- [10] R. C. Gonzalez, R. E. Woods, "Digital image processing, prentice hall," *Up. Saddle River, NJ*, 2008.
- [11] N. Kamolkunasiri, P. Punyabukkana, E. Chuangsuwanich, "A Comparative Study on Out of Scope Detection for Chest X-ray Images," in *20th International Joint Conference on Computer Science and Software Engineering*, Phitsanulok, Thailand, 2023, pp. 73-78. <https://doi.org/10.1109/JCSSE58229.2023.10202003>
- [12] M. Jha, Y. Hasija, "Artificial Intelligence In Field of Medical Imaging Informatics," in *3rd International Conference on Advance Computing and Innovative Technologies in Engineering*, Greater Noida, India, 2023, pp. 661-666. <https://doi.org/10.1109/ICACITE57410.2023.10182498>
- [13] O. Rodríguez-Bastidas, H. F. Vargas-Rosero, "Generation of 3D Tumor Models from DICOM Images for Virtual Planning of its Recession," *Revista Facultad de Ingeniería*, vol. 29, no. 54, e10173. <https://doi.org/10.19053/01211129.v29.n54.2020>
- [14] V. Göreke, "A novel method based on Wiener filter for denoising Poisson noise from medical X-Ray images," *Biomedical Signal Processing and Control*, vol.79, e104031, 2023. <https://doi.org/10.1016/j.bspc.2022.104031>

2D Gradient Algorithms for Noise Reduction in Radiological Images

- [15] S. Lee, M. G. Kang, "Poisson-Gaussian Noise Reduction for X-Ray Images Based on Local Linear Minimum Mean Square Error Shrinkage in Nonsampled Contourlet Transform Domain," *IEEE Access*, vol. 9, pp. 100637-100651, 2021. <https://doi.org/10.1109/ACCESS.2021.3097078>